## Piotr Wach

## Dynamics

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To my dear wife Irena

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## Notation Index

| $2 \pi / 3$ | se shift between 3-phase symmetrical sine curves |
| :---: | :---: |
| $\mathbf{a}=\dot{\mathbf{v}}=\ddot{\mathbf{r}}$ | - acceleration vector |
| $\delta A, \delta A_{m}, \delta A_{e}$ | - virtual work, its mechanical and electrical component |
| A | - vector potential of a magnetic field |
| $\mathbf{A}_{2}, \mathbf{A}_{3}$ | - skew symmetric matrices: 2- and 3-dimentional respectively |
| B | - magnetic induction vector |
| C | - electrical capacity |
| D | - viscous damping factor |
| $e_{k}$ | - electromotive force (EMF) induced in $k$-th winding |
| E | - total energy of a system |
| $f_{k}(\ldots)$ | - analytical notation of holonomic constraints function |
| F, $F_{i}$ | - vector of external forces, $i$-th component of this vector |
| $f_{L}, f_{s}, f_{r}$ | - frequency of voltage (current): feeding line, stator rotor |
| g | - acceleration vector of earth gravitation force |
| $g$ | - number of branches of electric network |
| $h$ | - number of holonomic constraints |
| $i=\dot{Q}$ | - electric current as a derivative of electrical charge |
| $i_{f}, i_{a}$ | - excitation current, armature current |
| $\underline{I}$ | - symbolic value of sinusoidal current |
| I | - matrix of inertia of a rigid body |
| $\mathbf{i}_{s}=\left[i_{s 1} i_{s 2} i_{s 3}\right]^{T}$ | - vector of a 3-phase stator currents |
| $\mathbf{i}_{s 12}=\left[i_{s 1} i_{s 2}\right]^{T}$ | - vector of a 3-phase stator currents in a star connected system |
| $\mathbf{i}_{r 13}=\left[i_{r 1} i_{r 3}\right]^{T}$ | - vector of a 3-phase rotor currents in a star connected system |
| $\mathbf{i}_{r}=\left[i_{r 1} i_{r 2} \ldots i_{m m}\right]^{T}$ | - vector of a m-phase rotor currents |
| $\mathbf{i}_{\text {souw }} \mathbf{i}_{\text {roww }}$ | - vectors of transformed stator, rotor currents in $0, u, v$ axes |
| $\mathbf{i}_{s v v}, \mathbf{i}_{r u v}$ | - vectors of transformed stator, rotor currents to $u, v$ axes |

